

Package: approximator (via r-universe)

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Type Package

Title Bayesian Prediction of Complex Computer Codes

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Description Performs Bayesian prediction of complex computer codes when fast approximations are available. It uses a hierarchical version of the Gaussian process, originally proposed by Kennedy and O'Hagan (2000), *Biometrika* 87(1):1.

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approximator-package *Bayesian approximation of computer models when fast approximations are available*

Description

Implements the ideas of Kennedy and O’Hagan 2000 (see references).

Details

Package: approximator
 Type: Package
 Version: 1.0
 Date: 2006-01-10
 License: GPL

This package implements the Bayesian approximation techniques discussed in Kennedy and O’Hagan 2000.

In its simplest form, it takes input from a “slow” but accurate code and a “fast” but inaccurate code, each run at different points in parameter space. The approximator package then uses both sets of model runs to infer what the slow code would produce at a given, untried point in parameter space.

The package includes functionality to work with a hierarchy of codes with increasing accuracy.

Author(s)

Robin K. S. Hankin

Maintainer: <hankin.robin@gmail.com>

References

R. K. S. Hankin 2005. “Introducing BACCO, an R bundle for Bayesian analysis of computer code output”, *Journal of Statistical Software*, 14(16)

M. C. Kennedy and A. O’Hagan 2000. “Predicting the output from a complex computer code when fast approximations are available” *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
mdash.fun(x=1:3, D1=D1.toy, subsets=subsets.toy, hpa=hpa.toy, z=z.toy, basis=basis.toy)
```

Afun

Matrix of correlations between two sets of points

Description

Returns the matrix of correlations of code output at each level evaluated at points on the design matrix.

Usage

```
Afun(level, Di, Dj, hpa)
```

Arguments

level	The level. This enters via the correlation scales
Di	First set of points
Dj	Second set of points
hpa	Hyperparameter object

Details

This is essentially a convenient wrapper for function `corr.matrix`. It is not really intended for the end user.

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

See Also

[corr,c_fun](#)

Examples

```
data(toyapps)
D2 <- D1.toy[subsets.toy[[2]],]
D3 <- D1.toy[subsets.toy[[3]],]

Afun(1,D2,D3,hpa.toy)
Afun(2,D2,D3,hpa.toy)
```

as.sublist	<i>Converts a level one design matrix and a subsets object into a list of design matrices, one for each level</i>
------------	---

Description

Given a level one design matrix, and a subsets object, convert into a list of design matrices, each one of which is the design matrix for its own level

Usage

```
as.sublist(D1, subsets)
```

Arguments

D1	Design matrix for level one code
subsets	subsets object

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
as.sublist(D1=D1.toy , subsets=subsets.toy)
```

`basis.toy`*Toy basis functions*

Description

A working example of a basis function

Usage

```
basis.toy(x)
```

Arguments

`x` Point in parameter space

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
basis.toy(D1.toy)
```

`betahat.app`*Estimate for beta*

Description

Returns the estimator for beta; equation 5. Function `betahat.app()` returns the estimate in terms of fundamental variables; `betahat.app.H()` requires the H matrix.

Usage

```
betahat.app.H(H, V = NULL, Vinv = NULL, z)
betahat.app(D1, subsets, basis, hpa, z, use.Vinv=TRUE)
```

Arguments

H	In <code>betahat.app.H()</code> , the H matrix, eg that returned by <code>H.fun()</code>
V	Variance matrix
Vinv	Inverse of variance matrix. If not supplied, it is calculated
use.Vinv	In function <code>betahat.app()</code> , a Boolean argument with default TRUE meaning to calculate the inverse of the V matrix; and FALSE meaning to use a method which does not involve calculating the inverse of V. The default method seems to be faster; YMMV
z	vector of observations
D1	Design matrix for level 1 code
subsets	Subsets object
basis	Basis function
hpa	Hyperparameter object

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)

betahat.app(D1=D1.toy, subsets=subsets.toy, basis=basis.toy, hpa=hpa.toy, z=z.toy, use.Vinv=TRUE)

H <- H.fun.app(D1=D1.toy, subsets=subsets.toy, basis=basis.toy, hpa=hpa.toy)
V <- V.fun.app(D1=D1.toy, subsets=subsets.toy, hpa=hpa.toy)
betahat.app.H(H=H, V=V, z=z.toy)
```

c.fun

Correlations between points in parameter space

Description

Correlation matrices between (sets of) points in parameter space, both prior (`c_fun()`) and posterior (`cdash.fun()`).

Usage

```
c_fun(x, xdash=x, subsets, hpa)
cdash.fun(x, xdash=x, V=NULL, Vinv=NULL, D1, subsets, basis, hpa, method=2)
```

Arguments

x, xdash	Points in parameter space; or, if a matrix, interpret the rows as points in parameter space. Note that the default value of xdash (viz x) will return the variance-covariance matrix of a set of points
D1	Design matrix
subsets	Subset object
hpa	hyperparameter object
basis	Basis function
V, Vinv	In function cdash.fun(), the data covariance matrix and its inverse. If NULL, the matrix will be calculated from scratch. Supplying a precalculated value for V, and especially Vinv, makes for very much faster execution (depending on method)
method	Integer specifying which of several algebraically identical methods to use. See the source code for details, but default option 2 seems to be the best. Bear in mind that option 3 does not require inversion of a matrix, but is not faster in practice

Value

Returns a matrix of covariances

Note

Do not confuse function c_fun(), which computes $c(x, x')$ defined just below equation 7 on page 4 with $c_t(x, x')$ defined in equation 3 on page 3.

Consider the example given for two levels on page 4 just after equation 7: $c(x, x') = c_2(x, x') + \rho_1^2 c_1(x, x')$ is a kind of prior covariance matrix. Matrix $c'(x, x')$ is a posterior covariance matrix, conditional on the code observations.

Function Afun() evaluates $c_t(x, x')$ in a nice vectorized way.

Equation 7 of KOH2000 contains a typo.

Author(s)

Robin K. S. Hankin

References

KOH2000

See Also

[Afun](#)

Examples

```

data(toyapps)

x <- latin.hypercube(4,3)
rownames(x) <- c("ash", "elm", "oak", "pine")
xdash <- latin.hypercube(7,3)
rownames(xdash) <- c("cod","bream","skate","sole","eel","crab","squid")

cdash.fun(x=x,xdash=xdash, D1=D1.toy, basis=basis.toy,subsets=subsets.toy, hpa=hpa.toy)

# Now add a point whose top-level value is known:
x <- rbind(x,D1.toy[subsets.toy[[4]][1],])

cdash.fun(x=x,xdash=xdash, D1=D1.toy, basis=basis.toy,subsets=subsets.toy, hpa=hpa.toy)
# Observe how the bottom row is zero (up to rounding error)

```

```
generate.toy.observations
```

Er, generate toy observations

Description

Generates toy observations on four levels using either internal (unknown) parameters and hyperparameters, or user-supplied versions.

Usage

```
generate.toy.observations(D1, subsets, basis.fun, hpa = NULL, betas = NULL,
export.truth = FALSE)
```

Arguments

D1	Design matrix for level 1 code
subsets	Subset object
basis.fun	Basis function
hpa	Hyperparameter object. If NULL, use the internal (true but unknown) hyperparameter object
betas	Regression coefficients. If NULL, use the internal (true but unknown) regression coefficients
export.truth	Boolean, with default FALSE meaning to return synthetic observations and TRUE meaning to return the actual hyperparameters and coefficients.

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O’Hagan 2000. “Predicting the output from a complex computer code when fast approximations are available” *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
generate.toy.observations(D1=D1.toy, subsets=subsets.toy, basis.fun=basis.toy)
```

genie

Genie datasets for approximator package

Description

Genie datasets that illustrate the package.

Format

The `genie` example is a case with three levels.

The `D1.genie` matrix is 36 rows of code run points, corresponding to the observations of the level 1 code. It has four columns, one per parameter.

`hpa.genie` is a hyperparameter object.

`subsets.genie` is a list of three elements. Element i corresponds to the rows of `D1.genie` at which level i has been observed.

`z.genie` is a three element list. Each element is a vector; element i corresponds to observations of level i . The lengths will match those of `subsets.genie`.

Function `basis.genie()` is a suitable basis function.

Function `hpa.fun.genie()` creates a hyperparameter object in a form suitable for passing to the other functions in the library.

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O’Hagan 2000. “Predicting the output from a complex computer code when fast approximations are available” *Biometrika*, 87(1): pp1-13

Examples

```
data(genie)
z.genie

jj <- list(trace=100,maxit=10)

hpa.genie.level1 <- opt.1(D=D1.genie, z=z.genie,
                        basis=basis.genie, subsets=subsets.genie,
                        hpa.start=hpa.genie.start,control=jj)

hpa.genie.level2 <- opt.gt.1(level=2, D=D1.genie, z=z.genie,
                             basis=basis.genie, subsets=subsets.genie,
                             hpa.start=hpa.genie.level1,control=jj)

hpa.genie.level3 <- opt.gt.1(level=3, D=D1.genie, z=z.genie,
                             basis=basis.genie, subsets=subsets.genie,
                             hpa.start=hpa.genie.level2,control=jj)
```

H.fun

The H matrix

Description

Returns the matrix of bases H. The “app” of the function name means “approximator”, to distinguish it from function H.fun() of the calibrator package.

Usage

```
H.fun.app(D1, subsets, basis, hpa)
```

Arguments

D1	Design matrix for level 1 code
subsets	Subsets object
basis	Basis function
hpa	Hyperparameter object

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O’Hagan 2000. “Predicting the output from a complex computer code when fast approximations are available” *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
H.fun.app(D1.toy , subsets=subsets.toy , basis=basis.toy , hpa=hpa.toy)
```

`hdash.fun`*Hdash*

Description

Returns the thing at the top of page 6

Usage

```
hdash.fun(x, hpa, basis)
```

Arguments

<code>x</code>	Point in question
<code>hpa</code>	Hyperparameter object
<code>basis</code>	Basis functions

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
hdash.fun(x=1:3 , hpa=hpa.toy,basis=basis.toy)

uu <- rbind(1:3,1,1:3,3:1)
rownames(uu) <- paste("uu",1:4,sep="_")
hdash.fun(x=uu, hpa=hpa.toy,basis=basis.toy)
```

`hpa.fun.toy`*Toy example of a hyperparameter object creation function*

Description

Creates a hyperparameter object from a vector of length 19. Intended as a toy example to be modified for real-world cases.

Usage

```
hpa.fun.toy(x)
```

Arguments

`x` Vector of length 19 that specifies the correlation scales

Details

Elements 1-4 of `x` specify the sigmas for each of the four levels in the toy example. Elements 5-7 specify the correlation scales for level 1, elements 8-10 the scales for level 2, and so on.

Internal function `pdm.maker()` shows how the `B` matrix is obtained from the various elements of input argument `x`. Note how, in this simple example, the `B` matrices are diagonal, but generalizing to non-diagonal matrices should be straightforward (if you can guarantee that they remain positive definite).

Value

<code>sigmas</code>	The four sigmas corresponding to the four levels
<code>B</code>	The four <code>B</code> matrices corresponding to the four levels
<code>rhos</code>	The three (sic) matrices corresponding to levels 1-3

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
hpa.fun.toy(1:19)
```

is.consistent	<i>Checks observational data for consistency with a subsets object</i>
---------------	--

Description

Checks observational data for consistency with a subsets object: the length of the vectors should match

Usage

```
is.consistent(subsets, z)
```

Arguments

subsets	A subsets object
z	Data

Value

Returns TRUE or FALSE depending on whether z is consistent with subsets.

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

See Also

[is.nested](#)

Examples

```
data(toyapps)
stopifnot(is.consistent(subsets.toy,z.toy))

z.toy[[4]] <- 1:6
is.consistent(subsets.toy,z.toy)
```

 mdash.fun

Mean of Gaussian process

Description

Returns the mean of the Gaussian process conditional on the observations and the hyperparameters

Usage

```
mdash.fun(x, D1, subsets, hpa, Vinv = NULL, use.Vinv = TRUE, z, basis)
```

Arguments

x	Point at which mean is desired
D1	Code design matrix for level 1 code
subsets	subsets object
hpa	Hyperparameter object
Vinv	Inverse of the variance matrix; if NULL, the function will calculate it
use.Vinv	Boolean, with default TRUE meaning to use the inverse of V and FALSE meaning to use a method that does not involve inverting V
z	observations
basis	Basis functions

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
mdash.fun(x=1:3,D1=D1.toy,subsets=subsets.toy,hpa=hpa.toy,z=z.toy,basis=basis.toy)

uu <- rbind(1:3,1,3:1,1:3)
rownames(uu) <- c("first","second","third","fourth")

mdash.fun(x=uu,D1=D1.toy,subsets=subsets.toy,hpa=hpa.toy,z=z.toy,basis=basis.toy)
```

 object

Optimization of posterior likelihood of hyperparameters

Description

Returns the likelihood of a set of hyperparameters given the data. Functions `opt1()` and `opt.gt.1()` find hyperparameters that maximize the relevant likelihood for level 1 and higher levels respectively. Function `object()` returns the expression given by equation 9 in KOH2000, which is minimized `opt1()` and `opt.gt.1()`.

Usage

```
object(level, D, z, basis, subsets, hpa)
opt.1(D, z, basis, subsets, hpa.start, give.answers=FALSE, ...)
opt.gt.1(level, D, z, basis, subsets, hpa.start, give.answers=FALSE, ...)
```

Arguments

<code>level</code>	level
<code>D</code>	Design matrix for top-level code
<code>z</code>	Data
<code>basis</code>	Basis function
<code>subsets</code>	subsets object
<code>hpa</code>	hyperparameter object
<code>hpa.start</code>	Starting value for hyperparameter object
<code>give.answers</code>	Boolean, with default FALSE meaning to return just the point estimate, and TRUE meaning to return extra information from the call to <code>optim()</code>
<code>...</code>	Extra arguments passed to <code>optim()</code> . A common one would be <code>control=list(trace=100)</code>

Details

This function is the object function used in toy optimizers `optimal.hpa()`.

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

See Also

[genie](#)

Examples

```

data(toyapps)
object(level=4, D=D1.toy , z=z.toy,basis=basis.toy,
  subsets=subsets.toy, hpa=hpa.fun.toy(1:19))
object(level=4, D=D1.toy , z=z.toy,basis=basis.toy,
  subsets=subsets.toy, hpa=hpa.fun.toy(3+(1:19)))

# Now a little example of finding optimal hyperparameters in the toy case
# (a bigger example is given on the genie help page)
jj <- list(trace=100,maxit=10)

hpa.toy.level1 <- opt.1(D=D1.toy, z=z.toy, basis=basis.toy,
  subsets=subsets.toy, hpa.start=hpa.toy,control=jj)

hpa.toy.level2 <- opt.gt.1(level=2, D=D1.toy, z=z.toy,
  basis=basis.toy, subsets=subsets.toy,
  hpa.start=hpa.toy.level1, control=jj)

hpa.toy.level3 <- opt.gt.1(level=3, D=D1.toy, z=z.toy,
  basis=basis.toy, subsets=subsets.toy,
  hpa.start=hpa.toy.level2, control=jj)

hpa.toy.level4 <- opt.gt.1(level=4, D=D1.toy, z=z.toy,
  basis=basis.toy, subsets=subsets.toy,
  hpa.start=hpa.toy.level3, control=jj)

```

 Pi

Kennedy's Pi notation

Description

Evaluates Kennedy's \prod product

Usage

Pi(hpa, i, j)

Arguments

hpa	Hyperparameter object
i	subscript
j	superscript

Details

This function evaluates Kennedy's \prod product, but with the additional feature that $\prod_i^j = 0$ if $i > j + 1$. This seems to work in practice.

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
Pi(hpa.toy,1,2)
Pi(hpa.toy,2,2)
Pi(hpa.toy,3,2)
Pi(hpa.toy,4,2)
```

subsets.fun

Generate and test subsets

Description

Create a list of subsets (`subsets.fun()`); or, given a list of subsets, test for correct inclusion (`is.nested()`), or strict inclusion (`is.strict()`).

Usage

```
is.nested(subsets)
is.strict(subsets)
subsets.fun(n, levels = 4, prob = 0.7)
```

Arguments

subsets	In <code>is.nested()</code> , a list of subsets to be tested
n	Number of observations in the lowest level (ie level 1, the fastest code)
levels	Number of levels
prob	Probability of choosing an observation at level $n + 1$ given that there is one at the same place at level n

Author(s)

Robin K. S. Hankin (`subsets.fun()`); Peter Dalgaard (via R-help)

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
is.nested(subsets.fun(20)) # Should be TRUE

data(toyapps)
stopifnot(is.nested(subsets.toy))
```

subset_maker

Create a simple subset object

Description

Given an integer vector whose i^{th} element is the number of runs at level i , return a subset object in echelon form.

Usage

```
subset_maker(x)
```

Arguments

`x` A vector of integers

Details

In this context, `x` being in “echelon form” means that

- `x` is consistent in the sense of passing `is.consistent()`
- For each i , `x[[i]] = 1:n` for some n .

Value

A list object suitable for use as a subset object

Author(s)

Robin K. S. Hankin

See Also

[is.consistent](#), [is.nested](#), [is.strict](#)

Examples

```
subset_maker(c(10,4,3))

is.nested(subset_maker(c(4,9,6))) #should be FALSE
is.nested(subset_maker(c(9,6,4))) #should be TRUE
```

tee.fun	<i>Returns generalized distances</i>
---------	--------------------------------------

Description

Returns generalized distances from a point to the design matrix as per equation 10

Usage

```
tee.fun(x, D1, subsets, hpa)
```

Arguments

x	Point in parameter space
D1	Design matrix for level 1 code
subsets	subsets object
hpa	Hyperparameter object

Details

See equation 10

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O'Hagan 2000. "Predicting the output from a complex computer code when fast approximations are available" *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
tee.fun(x=1:3, D1=D1.toy, subsets=subsets.toy, hpa=hpa.toy)
```

toyapps

Toy datasets for approximator package

Description

Toy datasets that illustrate the package.

Usage

```
data(toyapps)
```

Format

The toy example is a case with four levels.

The `D1.toy` matrix is 20 rows of code run points, corresponding to the observations of the level 1 code. It has three columns, one per parameter.

`hpa.toy` is a hyperparameter object. It is a list of three elements: `sigmas`, `B`, and `rhos`.

`subsets.toy` is a list of four elements. Element i corresponds to the rows of `D1.toy` at which level i has been observed.

`z.toy` is a four element list. Each element is a vector; element i corresponds to observations of level i . The lengths will match those of `subsets.toy`.

`betas.toy` is a matrix of coefficients.

Brief description of toy functions fully documented under their own manpage

Function `generate.toy.observations()` creates new toy datasets with any number of observations and code runs.

Function `basis.toy()` is an example of a basis function

Function `hpa.fun.toy()` creates a hyperparameter object such as `phi.toy` in a form suitable for passing to the other functions in the library.

See the helpfiles listed in the “see also” section below

Details

All toy datasets are documented here. There are also several toy functions that are needed for a toy problem; these are documented separately (they are too diverse to document fully in a single manpage). Nevertheless a terse summary for each toy function is provided on this page. All toy functions in the package are listed under “See Also”.

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O’Hagan 2000. “Predicting the output from a complex computer code when fast approximations are available” *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)

is.consistent(subsets.toy , z.toy)

generate.toy.observations(D1.toy, subsets.toy, basis.toy, hpa.toy, betas.toy)
```

V.fun.app

Variance matrix

Description

Given a design matrix, a subsets object and a hyperparameter object, return the variance matrix. The “app” of the function name means “approximator”, to distinguish it from function V.fun() of the calibrator package.

Usage

```
V.fun.app(D1, subsets, hpa)
```

Arguments

D1	Design matrix for level 1 code
subsets	Subsets object
hpa	Hyperparameter object

Author(s)

Robin K. S. Hankin

References

M. C. Kennedy and A. O’Hagan 2000. “Predicting the output from a complex computer code when fast approximations are available” *Biometrika*, 87(1): pp1-13

Examples

```
data(toyapps)
V.fun.app(D1.toy, subsets.toy, hpa.toy)
```

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